

Bioinformatics 1

Population variation

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DNA damage

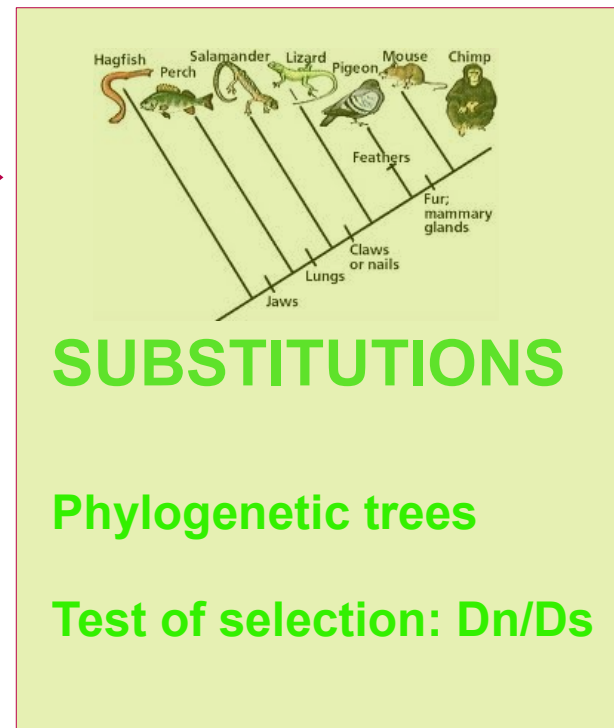
Copying errors

MUTATIONS: heritable changes to the genome,
essential for evolution.



POLYMORPHISMS

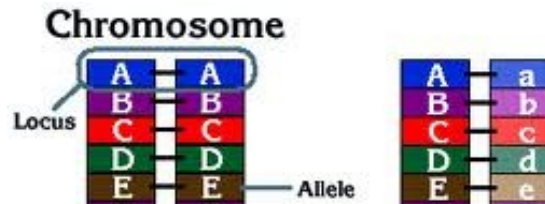
?





How much variation is out there, and how does it evolve over time ?

A useful way of looking at it:
ALLELE FREQUENCIES

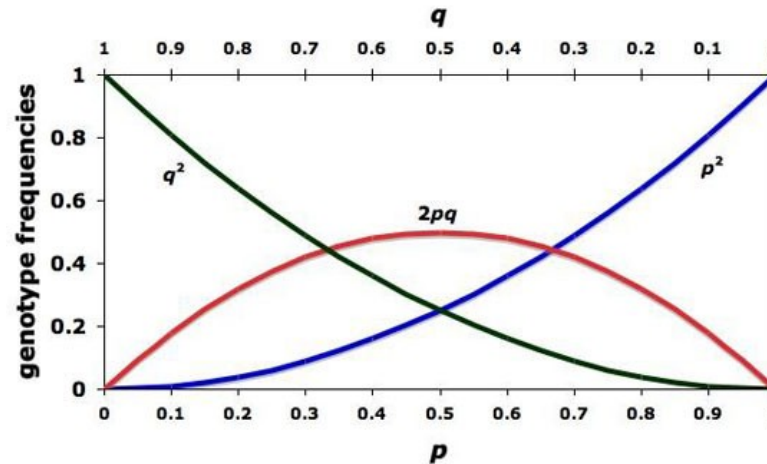


Do allele frequencies change over time? If so, how and why?

Ideal baseline: HARDY-WEINBERG EQUILIBRIUM MODEL

Hp) Infinite population
Random mating
No selection
No migration

Ts) Allele frequencies
are constant



Nucleotide diversity: a measure of the degree of polymorphism within a population

```
subj0    ATAATAAAAA AATAATAAAA AAATAAAAAA AATAAAAAAA A
subj1    AAAAAAATA AATAATAAAA AAATAAAAAA AAAAAAATAA A
subj2    AAAATAAAAA TATAATAAAA AAATATAAAA AAAAAAATAA A
subj3    AAAAAAATA AATAATAAAA AAATAAATAA ATAAAAAATA A
subj4    AAAATAAAAA AAATATAAAA AAATAAAAAA AAAAAAATAA A
subj5    AAAATAAAAA AAAAAATAAA AAAAAAATAA AAAAAATAAA A
subj6    AAAAAATAAA AATAATAAAA AAATAAAAAA AAAAAAATAA A
subj7    AAAAAAATA AAAAAATAAA AAATAAAAAA AAAAAAATAA A
subj8    AAAAAAATA AAAAAATAAA AAATAAAAAA AAAAAAATAA A
subj9    AAAAAAATA AAAAAATAAA AAATAAATAA AAAAAAATAA A
```

Average number of nucleotide differences per site between any two DNA sequences chosen randomly from the sample population, and is denoted by π .

Tajima's D

$$E[\pi] = \theta$$

$$E[S] = a_1 \theta$$

$\theta = 4N u$ ($2N$ = haploid population size, u = mutation rate/generation), and a_1 is defined below.

$$D = \frac{\pi - S/a_1}{\sqrt{e_1 S + e_2 S(S-1)}}$$

A negative Tajima's D signifies an excess of low frequency polymorphisms relative to expectation, indicating population size expansion (e.g., after a bottleneck or a selective sweep) and/or purifying selection.

A positive Tajima's D signifies low levels of both low and high frequency polymorphisms, indicating a decrease in population size and/or balancing selection.

Pop size matters

$$N_e s < 1$$

Neutral mutations

At selectively neutral sites, the rate of substitution is equal to the rate of mutation

$$K = Nu \times 1/N = u$$

u = rate of mutation per generation

N = Pop size

K = rate of substitution per generation



Statistical measures of rate of Syn NonSyn substitutions

Approximation:

1st + 2nd vs. 3rd codon positions

Count number of Syn and NonSyn sites!

Exact calculation based on the genetic code

$$D_s = \# \text{ Syn Subst} / \# \text{ Syn sites}$$

$$D_n = \# \text{ NonSyn Subst} / \# \text{ NonSyn sites}$$



What do we expect?

Synonymous substitution to be more frequent than Nonsynonymous substitutions

Rate of Synonymous substitutions to be more similar between genes than the rate of Nonsynonymous substitutions



Dn/Ds measure of positive selection

Sliding window approach to detect local signal of positive selection

Neutral Evolution $D_N / D_s = 1$

Positive Darwinian selection $D_N / D_s > 1$

Negative purifying selection $D_N / D_s < 1$

Mc Donald Kreitmann test

Main idea: genetic variability between populations
should be correlated with that within populations

	Fixed	Polymorphic
Synonymous	Ds	Ps
Nonsynonymous	Dn	Pn

Further levels....

Expression: allele specificity, tissue specificity

Epigenomics

new kinds of data: discrete (methylation states) and continuous (chromatin structure)

different relevant time scales

intra(!)-individual variability

modes of heritability

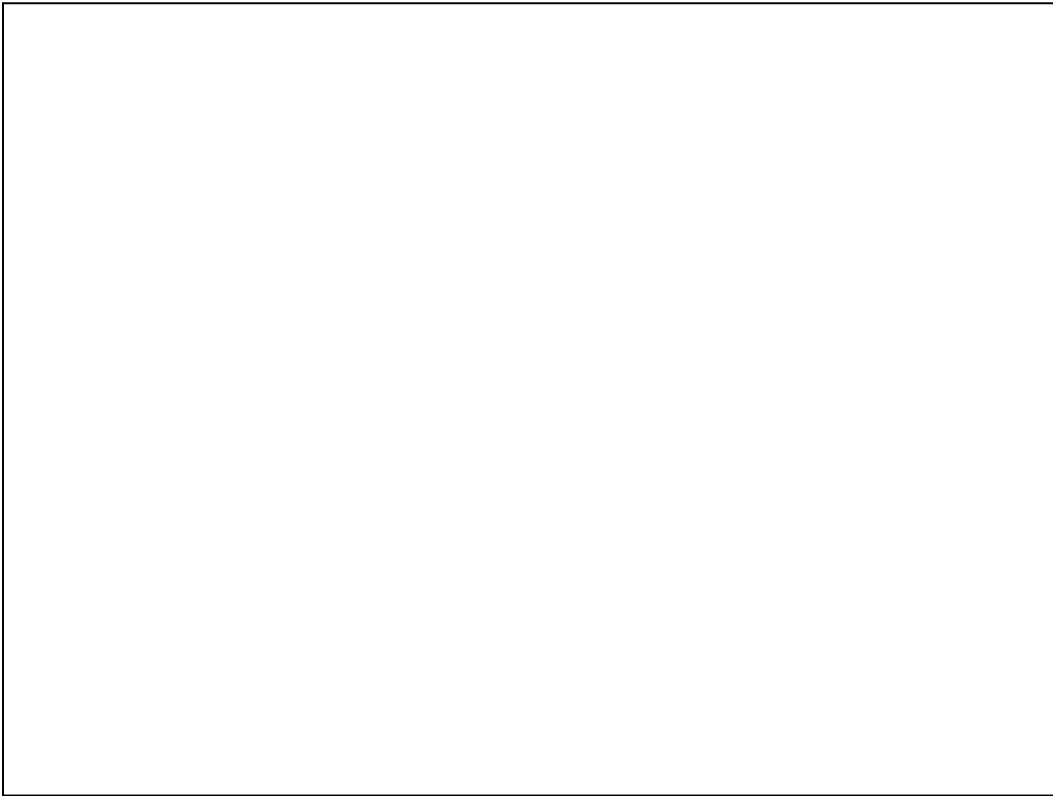
imprinting

non-Mendelian inheritance - meiotic drive



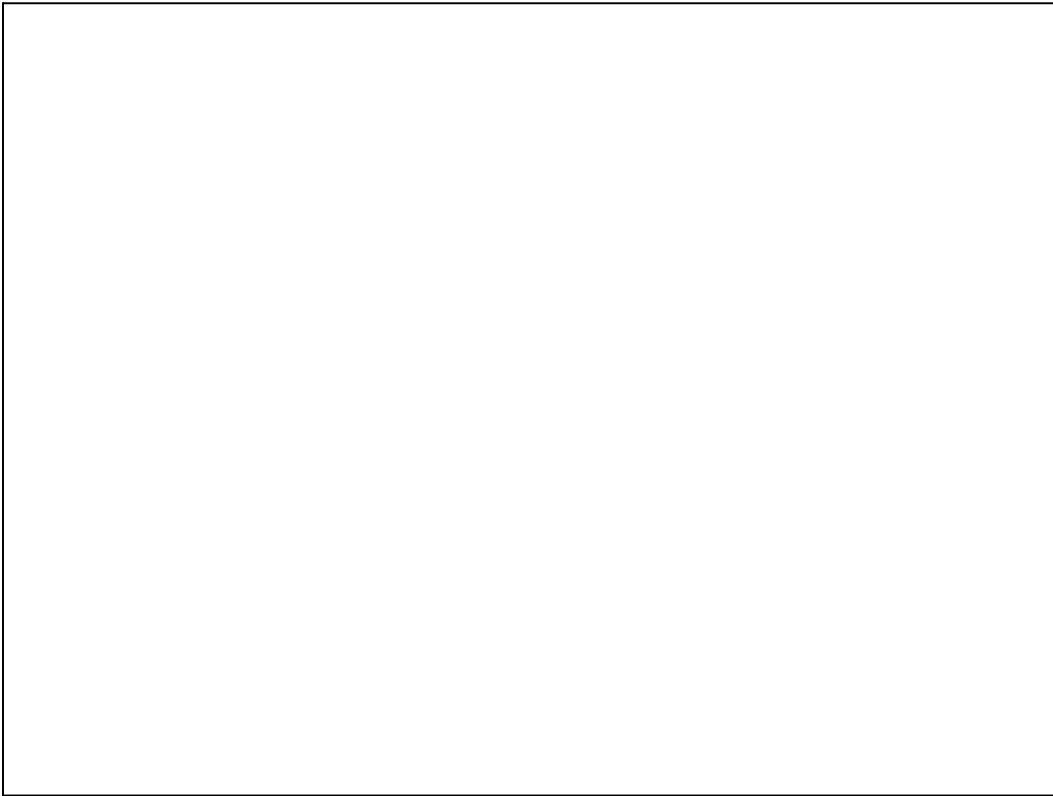






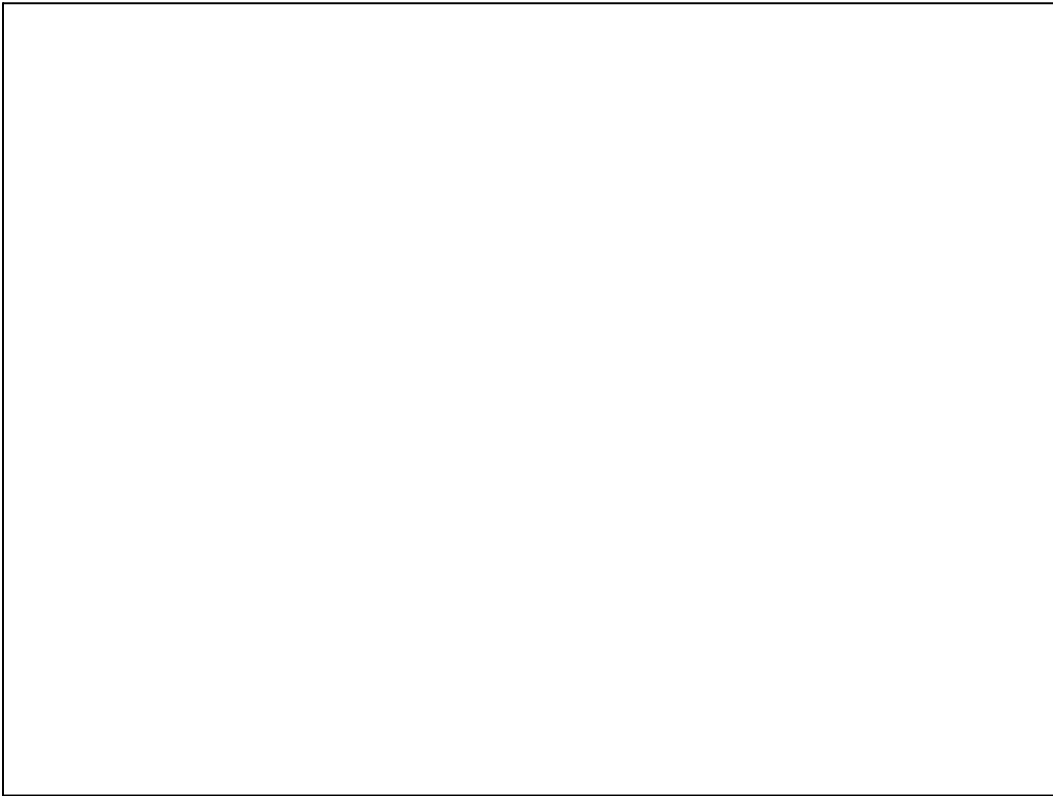
The Hardy-Weinberg theorem characterizes the distributions of genotype frequencies in populations that are not evolving, and is thus the fundamental null model for population genetics.

Evolution can be defined as the change in allele frequencies (i.e., genotypes) over time. In the early 1900s, G. Hardy and W. Weinberg developed a mathematical model that predicts genotype frequencies when a population is not being affected by evolutionary forces. The model is known as the Hardy Weinberg Equilibrium Model. The Hardy-Weinberg equilibrium is a baseline against which the evolution of populations can be measured and is the foundation for the genetic theory of evolution. When a population is in Hardy-Weinberg equilibrium, there is no change in gene frequencies and, therefore, no evolution of the population. The conditions required for Hardy-Weinberg equilibrium are almost never met in nature, however. As a result, gene frequencies change and evolution occurs. If a population is not at Hardy-Weinberg equilibrium, then we know that one or more of the conditions required for the equilibrium are not being met.



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